

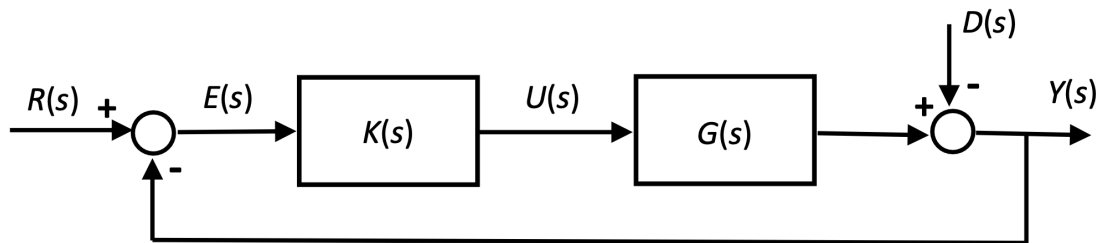
## Automatic Control Systems – February 21, 2024

Student: \_\_\_\_\_ ID: \_\_\_\_\_

1. Given the LTI system defined by the transfer function  $G(s)$ ,

$$G(s) = \frac{4(10s + 5)}{(s^2 + 22s + 40)},$$

- a. calculate the analytic expression of the forced response to a step input of unitary amplitude (i.e., step response);
  - b. draw the qualitative step response.
2. For the closed loop system shown in figure,



where

$$G(s) = \frac{1}{(s + 1)(s + 3)},$$

- a. devise  $K(s)$  in order to satisfy the following requirements:
  - i.  $e_{\infty} = 0$  in the presence of both reference,  $r(t)$ , and disturbance,  $d(t)$ , step input signals;
  - ii.  $y(t)$  without showing overshoot;
  - iii. settling time  $t_{s5\%} \leq 3$  s;
- b. draw the qualitative response  $y(t)$  of the devised closed loop system to the following inputs:

$$r(t) = 1(t);$$

$$d(t) = 0.3 \cdot 1(t - 6).$$

**Time available: 2 hours**