



UNIVERSITÀ DEGLI STUDI DI NAPOLI
PARTHENOPE

Artificial Intelligence

Knowledge Representation and Inference

LESSON 10

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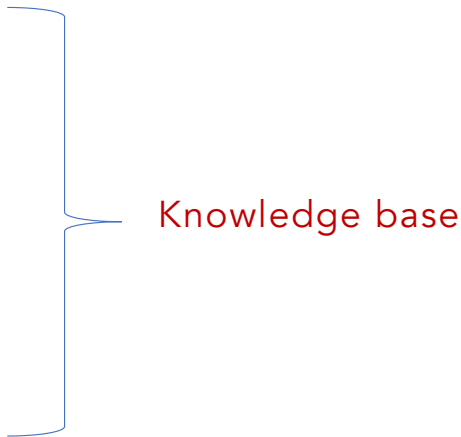
Knowledge-based Agents

- Human intelligence is based on **knowledge**
 - People know information and facts about the world
 - Using that information, people draw conclusions
- Our interest is to focus on the ability to reason based on knowledge when applied to artificial intelligence
- We're going to develop what are known as **knowledge-based agents**
 - Agents that reason by operating on the **internal representation of knowledge**

Knowledge-Based Agents

- The core of a knowledge-based agent is the **knowledge base**
 - A set of sentences
- A sentence is expressed in a **knowledge representation language**
 - It represents an assertion about the world
- If a sentence is given without being derived from other sentences it is called an **axiom**
- Drawing conclusions, that is, deriving new sentences from the knowledge base is done through **inference**

Example from Harry Potter Saga

- Let's take one sentence that **we know to be true**
 - *If it didn't rain, Harry visited Hagrid today*
 - Then take another fact
 - *Harry visited Hagrid or Dumbledore today, but not both*
 - Finally, consider a third piece of information
 - *Harry visited Dumbledore today*
- 
- Knowledge base
- From this knowledge base, we can try to reason to draw some conclusion
 - *Harry did not visit Hagrid today*
 - *It rained today*
 - It's this kind of reasoning, logical reasoning, where humans use logic based on the known information to enrich that information and draw conclusions

Human Reasoning vs Computer Reasoning

- Humans reason about logic generally in terms of human language
 - For instance, focusing on the English language, given a few sentences we try to reason through how it is that they relate to one another
- With computers, we need to be more formal
 - It is necessary to encode the notion of *logic*, and *truth* and *falsehood* inside a machine
- Introduction of a few more terms and a few symbols that will help us to realize the notion of logic inside of artificial intelligence

Logic

- A sentence in a natural language like English is just something that one is saying
- In the context of AI a sentence is
 - An assertion about the world in a **knowledge representation language**
 - some way of representing knowledge inside of computers

Knowledge-based Agents

- The knowledge base may be
 - extended with new sentences
 - An operation we can call TELL
 - Queried on what is known
 - An operation called ASK
- Inference satisfies the requirement that when one ASKs a question to the knowledge base, the answer should follow from what has been told (or TELLED) previously to KB
- The agent takes a percept as input and returns an action
 - The agent maintains a knowledge base, KB
 - KB contains some background knowledge

function KB-AGENT(*percept*) **returns** an *action*
persistent: *KB*, a knowledge base
t, a counter, initially 0, indicating time

```
TELL(KB, MAKE-PERCEPT-SENTENCE(percept, t))  
action ← ASK(KB, MAKE-ACTION-QUERY(t))  
TELL(KB, MAKE-ACTION-SENTENCE(action, t))  
t ← t + 1  
return action
```

Knowledge-based Agents

- When the agent program is called, it
 1. **TELLs** the knowledge base what it perceives
 2. **ASKs** the knowledge base what action it should perform
 - Answering the query, a reasoning process may occur involving the current state of the world, the outcomes of possible action sequences, ...
 3. **TELLs** the knowledge base of the chosen action and returns the action to execute
- **MAKE-PERCEPT-SENTENCE** constructs a sentence asserting that the agent perceived the given percept at the given time
- **MAKE-ACTION-QUERY** constructs a sentence that asks what action should be done at the current time
- **MAKE-ACTION-SENTENCE** constructs a sentence asserting that the chosen action was executed

```
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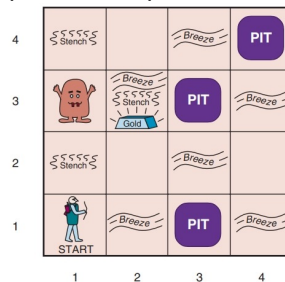

Some other examples

- Automatic theorem proving
 - Write a computer program capable to prove or to refute the following statement
 - Goldbach's conjecture (1742)
 - *For any even number $p \geq 4$, there exists at least one pair of prime numbers q and r (identical or not) such that*

$$q + r = p$$

Some other examples

- Game playing
 - Write a computer program capable of playing the Wumpus game, a text-based computer game used in a modified version as an AI's toy-problem
 - Basic version
 - The **Wumpus world**: a cave made up of connected rooms, bottomless pits, a heap of gold, and the Wumpus, a beast that eats anyone who enter its room
 - **Goal**: starting from room (1,1), find the gold and go back to (1,1), without falling into a pit or hitting the Wumpus
 - Main **rules of the game**:
 - The content of any room is known only after entering it
 - In rooms neighboring the Wumpus and pits a **stench** and a **breeze** are perceived, respectively

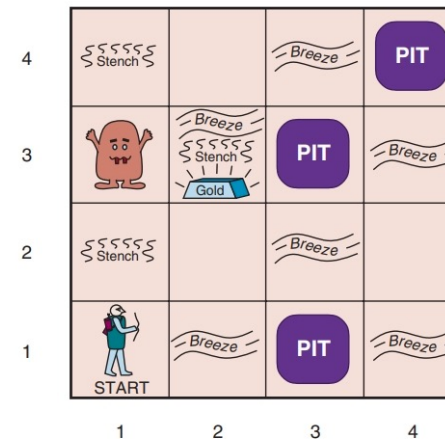


Knowledge-based Systems

- Humans usually solve problems like the ones above by combining high-level abstract **knowledge representation** and **reasoning**
- **Knowledge-based systems** aim at automating the human capabilities
 - Representing knowledge about the world
 - Reasoning to derive new knowledge and to guide action

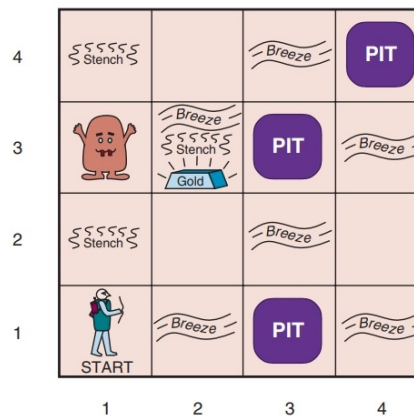
Wumpus World Description (PEAS)

- **Performance measure**
 - gold +1000, death -1000
 - -1 per step, -10 for using the arrow
- **Environment**
 - Squares adjacent to wumpus are smelly
 - Squares adjacent to pit are breezy
 - Glitter iff gold is in the same square
 - Shooting kills Wumpus if you are facing it
 - Shooting uses up the only arrow
 - Grabbing picks up gold if in the same square
 - Releasing drops the gold in the same square
- **Actuators**
 - Left turn, Right turn, Forward, Grab, Release, Shoot
- **Sensors**
 - Breeze, Glitter, Smell



Playing the Wumpus Game

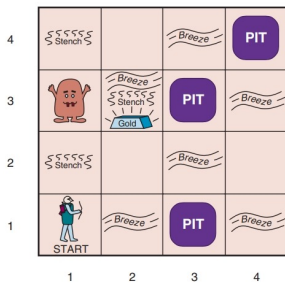
- Consider the following initial configuration of the Wumpus game, and remember that the content of any room is known only after entering it



- If you are the player, how would you reason to decide the next move to do at each game step?

Exploring a Wumpus World

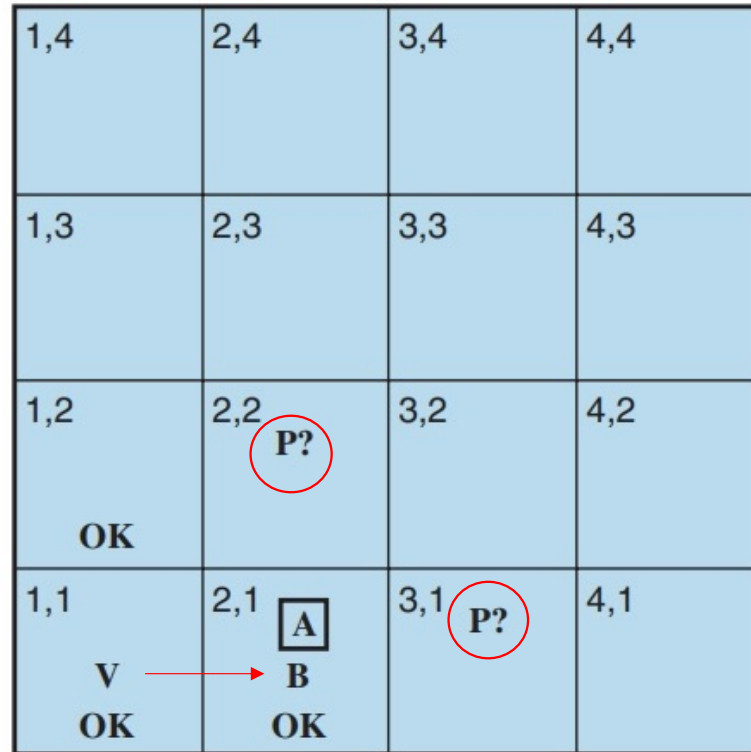
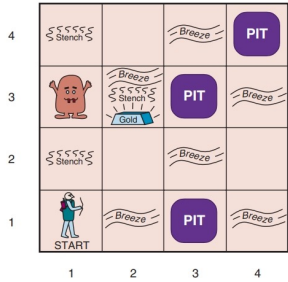
- Sketch of a possible reasoning process for deciding the next move



1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3
1,2	2,2	3,2	4,2
1,1	2,1	3,1	4,1
OK	OK		

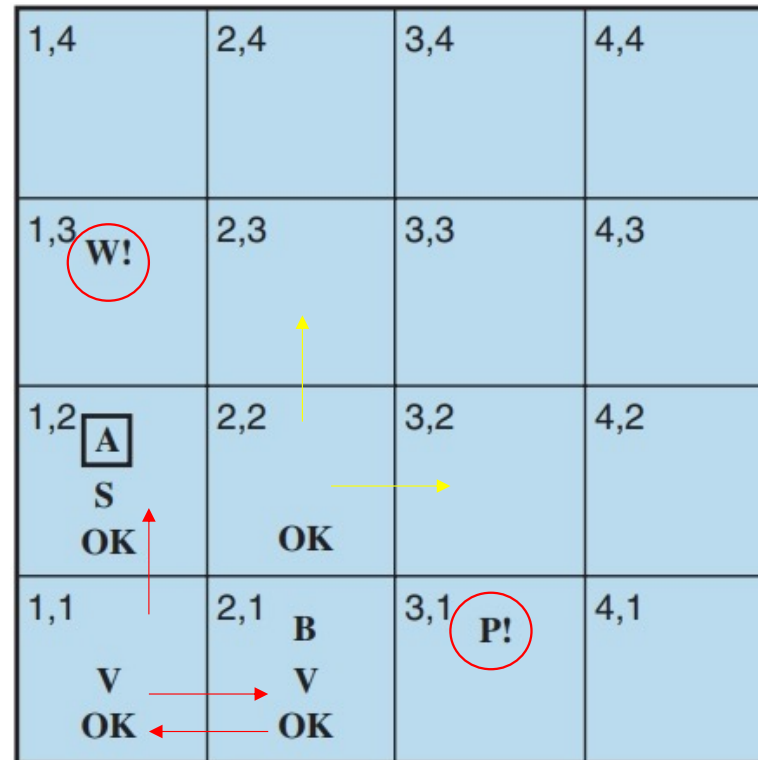
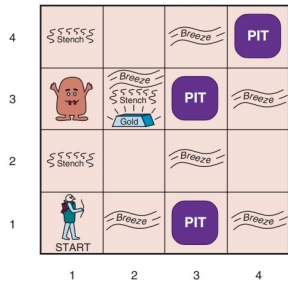
A = Agent
B = Breeze
G = Glitter, Gold
OK = Safe square
P = Pit
S = Stench
V = Visited
W = Wumpus

Exploring a Wumpus World



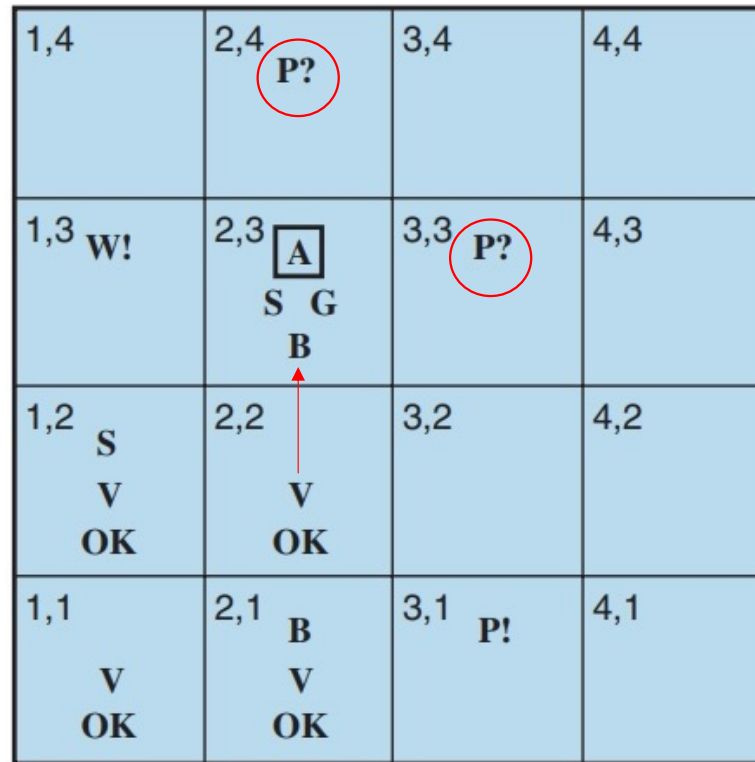
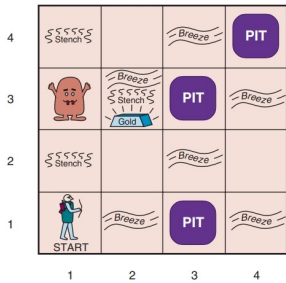
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Exploring a Wumpus World



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Main Approaches to AI system Design

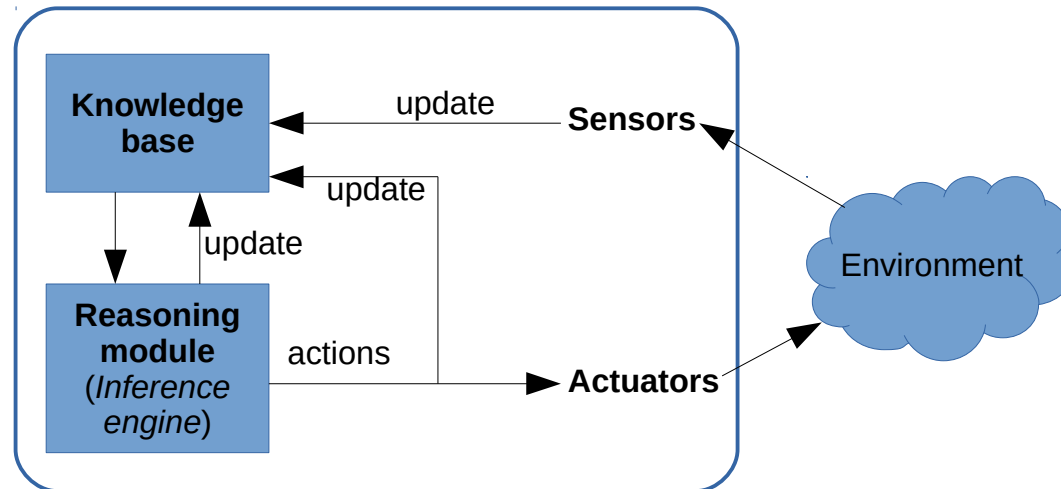
- Procedural

- The desired behavior (actions) are encoded directly as program code
 - No explicit knowledge representation and reasoning

- Declarative

- Explicit representation, in a **knowledge base**, of
 - **Background knowledge** (e.g., the rules of the Wumpus game)
 - Knowledge about one specific **problem instance** (e.g., what the agent knows about a specific Wumpus cave it is exploring)
 - The agent's **goal**
- Actions are then derived from **reasoning**

Architecture of Knowledge-based Systems



- A peculiar characteristic is a **separation** between knowledge representation and reasoning
 - The **knowledge base** contains all the agent's knowledge about its environment, in a **declarative** form
 - The **inference engine** implements a reasoning process to derive new knowledge and to make decisions

Knowledge Representation and Reasoning

- Logic is one of the main tools used in AI for
 - Knowledge representation
 - Logical languages
 - Propositional logic
 - Predicate (first-order) logic
 - Reasoning
 - Inference rules and algorithms
- Inherited contributions
 - Aristotle (4th century BC): the “laws of thought”
 - G. Boole (1815-64): Boolean algebra (propositional logic)
 - G. Frege (1848-1925): predicate logic
 - K. Gödel (1906-78): incompleteness theorem

Main Applications

- Automatic theorem provers
- Logic programming languages (e.g., Prolog)
- Expert Systems



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Logic



Logic

- The study of conditions under which an **argumentation** (reasoning) is **correct**
- The concepts involved in the above definition
 - **Argumentation**
 - A set of statements consisting of some premises and one conclusion:
 - *All men are mortal; Socrates is a man; then, Socrates is mortal*
 - **Correctness**
 - When the conclusion cannot be *false* when all the premises are true
 - **Proof**
 - A procedure to assess the correctness

Propositions

- Natural language is very complex and vague \Rightarrow hard to formalize
- Logic considers argumentations made up of only a subset of statements
 - **Propositions** (declarative statements)
 - A *proposition* is a statement expressing a concept that can be either *true* or *false*
- Example
 - *Socrates is a man*
 - *Two and two makes four*
 - *If the Earth had been flat, then Columbus would have not reached America*

Simple and Complex Propositions

- A proposition is
 - **Simple**, if it does not contain simpler propositions
 - **Complex**, if it is made up of simpler propositions connected by logical connectives
- Example
 - **Simple** propositions
 - *Socrates is a man*
 - *Two and two makes four*
 - **Complex** propositions
 - *A basketball match can be won **or** lost*
 - *If the Earth had been flat, **then** Columbus would have not reached America*

Argumentations

- When can a proposition be considered true or false?
 - This is a **philosophical** question
 - Logic does not address this question: it only analyzes the **structure** of argumentation
- Example
 - *All men are mortal; Socrates is a man; then, Socrates is mortal*
 - Informally, the **structure** of this argumentation is:
 - All P are Q; x is P; then x is Q
- Is it correct, **whatever** P, Q, and x are, that is, **regardless** of whether the corresponding propositions "all P are Q", "x is P" and "x is Q" are true or false?

Formal Languages

- Logic provides **formal languages** for representing propositions in the form of **sentences**
- A formal language is defined by **syntax** and **semantics**
 - **Syntax** (grammar)
 - Rules that define what sentences are well-formed
 - **Semantics**
 - Rules that define the meaning of well-formed sentences
 - The truth of sentences with respect to each possible world
- Examples (of formal languages)
 - Arithmetic: propositions about numbers
 - Programming languages: instructions to be executed by a computer
- Logicians typically think in terms of **models**, which are formally structured worlds with respect to which truth can be evaluated
 - We say m is a **model** of a sentence α if α is *true* in m
 - $M(\alpha)$ is the set of all models of α

Natural vs Logical Languages

- Natural languages
 - Syntax is not rigorously defined
 - Semantics defines the content of a statement, i.e., what it refers to in the real world
- Example (syntax)
 - *The book is on the table*: syntactically correct statement, with a clear semantics
 - *Book the on is table the*: syntactically incorrect statement, no meaning can be attributed to it
 - *Colorless green ideas sleep furiously*: syntactically correct, but what does it mean?

Natural vs Logical Languages

- Logical languages
 - Syntax
 - formally defined
 - Semantics
 - Rules that define the **truth value** of each well-formed sentence w.r.t. each possible **model** (a possible world represented by that sentence)
- Example
 - **Syntax**
 - $x + y = 4$ is a well-formed sentence, $x4y + =$ is not
 - **Model**
 - The symbol 4 represents the natural number four, x and y any pair of natural numbers, + the sum operator, etc.
 - **Semantics**
 - $x + y = 4$ is true for $x = 1$ and $y = 3$, $x = 3$ and $y = 2$, etc.

Logical Entailment

- Logical reasoning is based on the relation of **logical entailment** between sentences
 - Defines when a sentence **logically follows** from one another

- **Definition**

- The sentence α **entails** the sentence β if and only if in every model in which α is true, also β is true

$$\alpha \models \beta$$

- **Example (arithmetic)**

- $x + y = 4 \models x = 4 - y$
 - In every model (i.e., for any assignment of numbers to x and y) in which $x + y = 4$ is *true*, also $x = 4 - y$ is *true*

Logical Inference

- **Logical inference**
 - *The process of deriving conclusions from premises*
- **Inference algorithm**
 - *A procedure that derives sentences (conclusions) from other sentences (premises) in a formal language*
- Formally, the fact that an inference algorithm A derives a sentence α from a set of sentences (**knowledge base**) KB is written as

$$KB \vdash_A \alpha$$

Properties of Inference Algorithms

- Definition

- Soundness (truth preservation)

- If an inference algorithm derives **only** sentences entailed by the premises, i.e.:

$$\text{if } KB \vdash_A \alpha, \text{ then } KB \models \alpha$$

- Completeness

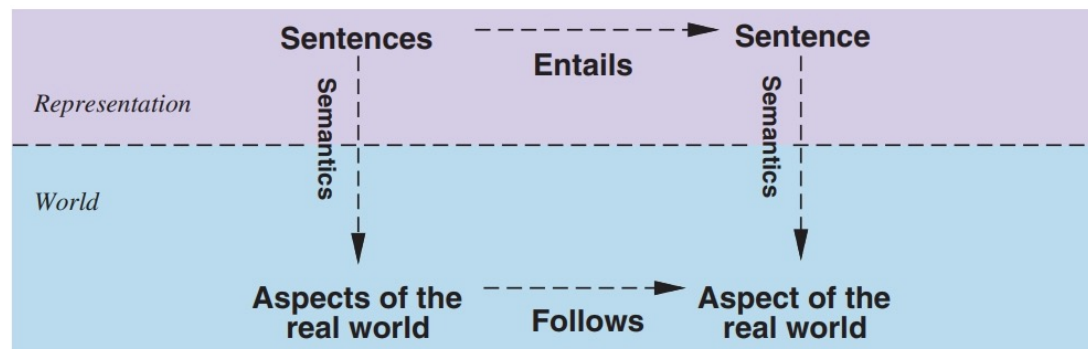
- If an inference algorithm derives **all** the sentences entailed by the premises, i.e.:

$$\text{If } KB \models \alpha, \text{ then } KB \vdash_A \alpha$$

- A **sound** algorithm derives conclusions that are guaranteed to be true in any world in which the premises are true

Properties of Inference Algorithms

- Inference algorithms operate only at the **syntactic** level:
 - sentences are physical configurations of an agent (e.g., bits in registers)
 - inference algorithms construct new physical configurations from previous ones
 - logical reasoning should ensure that new configurations represent aspects of the world that actually follow from the ones represented by previous configurations



Applications of Inference Algorithms

- In AI inference is used to answer two main kinds of questions
 - Does a **given** conclusion α logically follow from the agent's knowledge KB? That is, $KB \models \alpha$
 - What are **all** the conclusions that logically follow from the agent's knowledge? That is, find all α such that $KB \models \alpha$
- Example
 - Does a breeze in room (2,1) entail the presence of a pit in room (2,2)?
 - What conclusions can be derived about the presence of pits and of the Wumpus in each room, from the current knowledge?

1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3
1,2	2,2 p?	3,2	4,2
OK			
1,1 v OK	2,1 A B OK	3,1 p?	4,1

Inference Algorithms: Model Checking

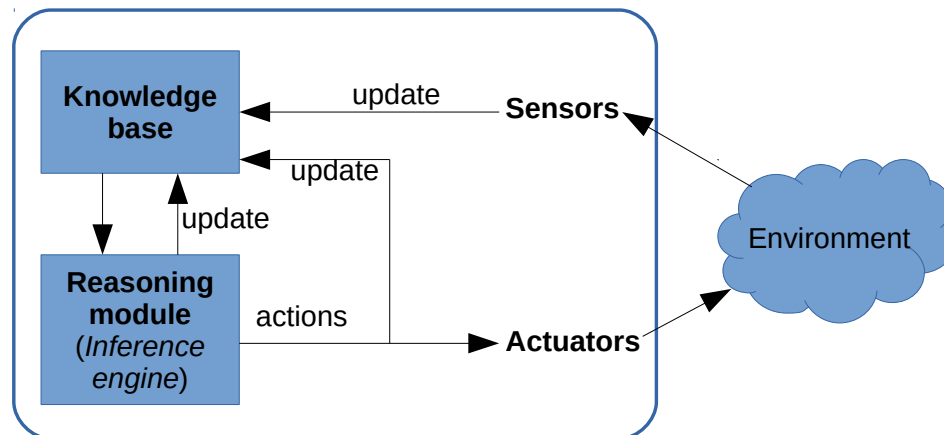
- The definition of **entailment** can be directly applied to construct a simple inference algorithm, named **Model checking**
 - Given a set of premises, KB , and a sentence α , **enumerate** all possible models and **check** whether α is *true* in **every** model in which KB is *true*
- **Example (arithmetic)**
 - $KB : \{x + y = 4\}$
 - $\alpha : y = 4 - x$
 - Is the inference $\{x + y = 4\} \vdash y = 4 - x$ correct?
 - **Model checking**: enumerate all possible pairs of numbers x, y , and check whether $y = 4 - x$ is true whenever $x + y = 4$ is

The Issue of Grounding

- A knowledge base *KB* is just “syntax” (a physical configuration of the agent):
 - what is the connection between a *KB* and the real world?
 - how does one know that *KB* is true in the real world?
- This is a **philosophical** question. For humans:
 - a set of beliefs (set of statements considered true) is a physical configuration of our brain
 - how do we know that our beliefs are true in the real world?
- A simple answer can be given for agents (e.g., computer programs or robots): the connection is created by
 - **sensors**, e.g.: perceiving a breeze in the wumpus world
 - **learning**, e.g., when a breeze is perceived, there is a pit in some adjacent room
 - Of course, both perception and learning are **fallible**

Architecture of Knowledge-based Systems Revisited

- If logical language is used
 - **Knowledge base**
 - A set of sentences in a given logical language
 - **Inference engine**
 - An inference algorithm for the same logical language



Logical Languages

- **Propositional logic**
 - The simplest logic language
 - An extension of Boolean algebra
- **Predicate (or first-order) logic**
 - A more expressive and concise extension of propositional logic
 - Seminal work by Frege