



**SIS** Scuola Interdipartimentale  
delle Scienze, dell'Ingegneria  
e della Salute



L. Magistrale in IA (ML&BD)

**Scientific Computing  
(part 2 – 6 credits)**

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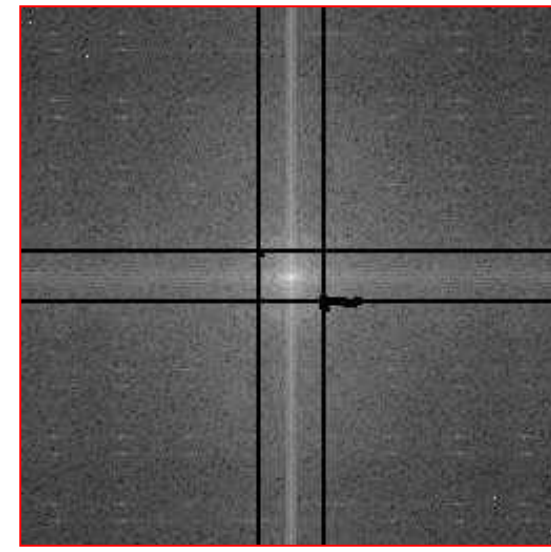
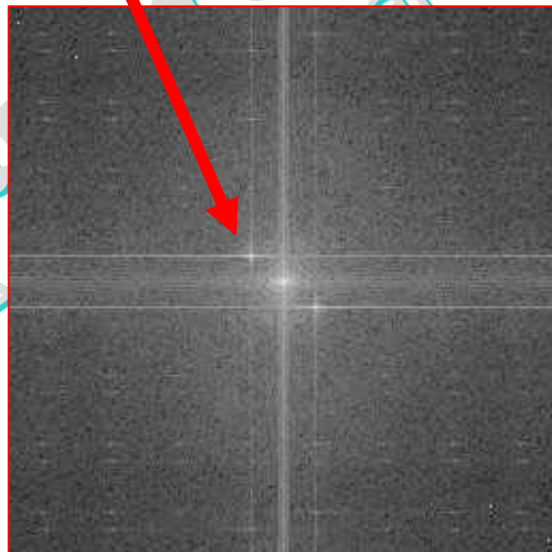
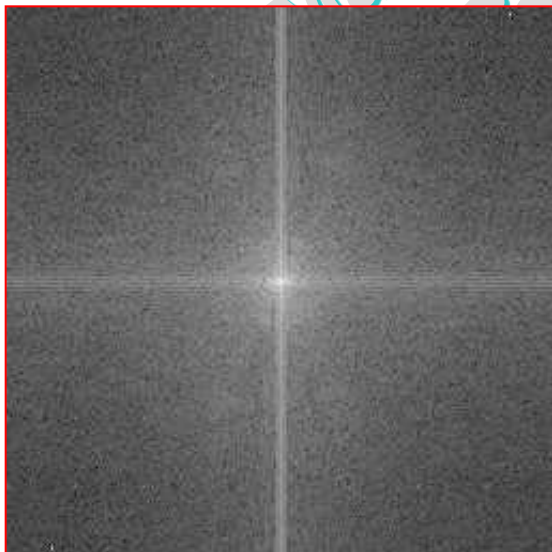
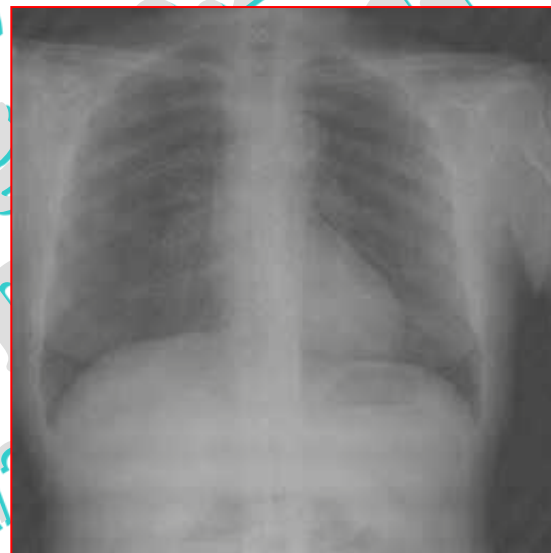
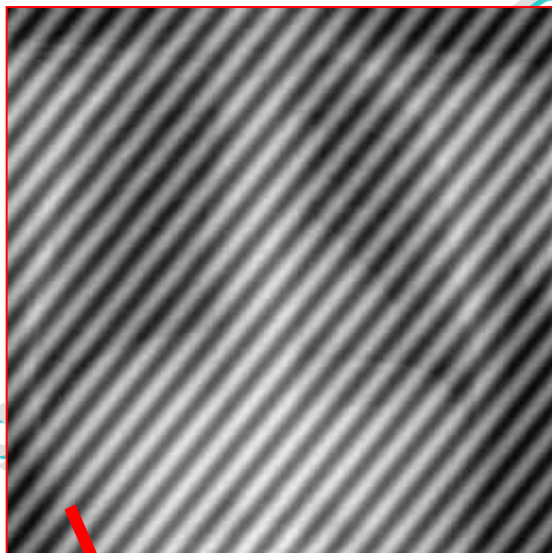
# Contents

- **Other applications of 2D FT to images.**

from the previous  
MATLAB examples

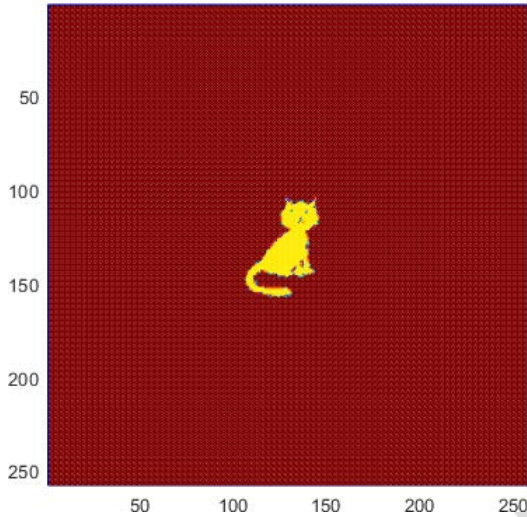
# APPLICATION: remove periodic noise

remove periodic noise

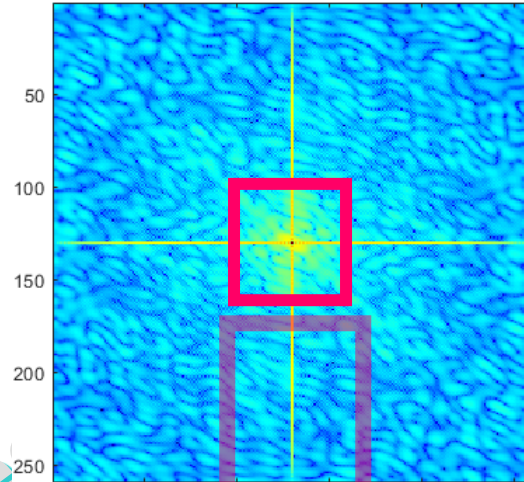


# Example: windowing in frequency domain

Original image

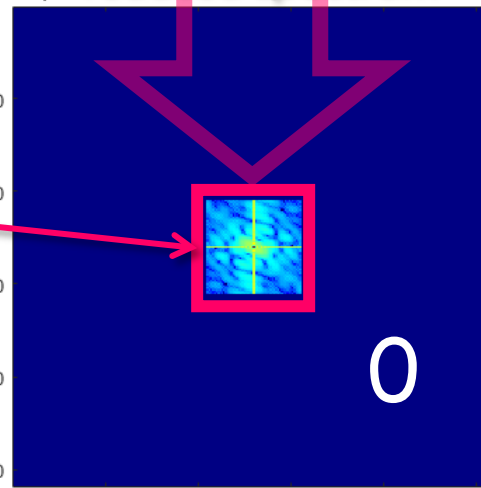


Fourier spectrum



secondary oscillations

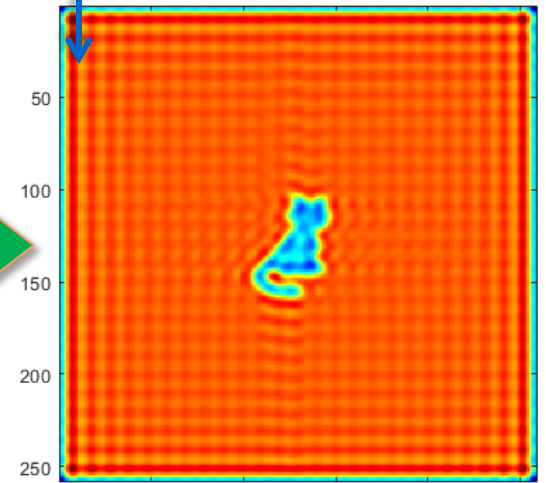
`imagesc(uint8(abs(...)))`  
reduced spectrum



window

reconstructed image

Reconstruction from reduced FT of size 51 x 51

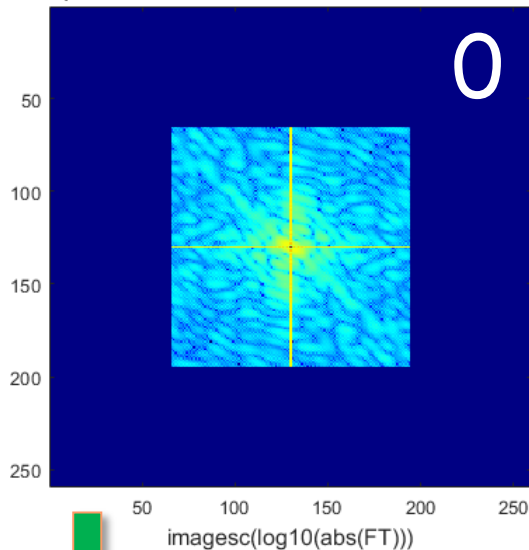


**Question:** What do you expect with a smaller window? And with a larger one?

# Example: windowing in frequency domain

reduced Spectrum

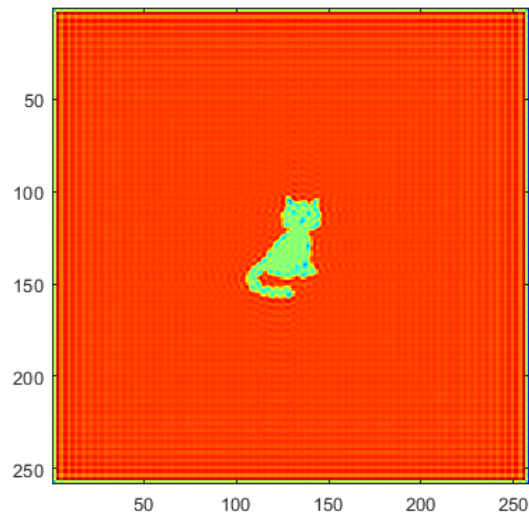
Spectrum of reduced FT of size 129 x 129



larger window

reconstructed image

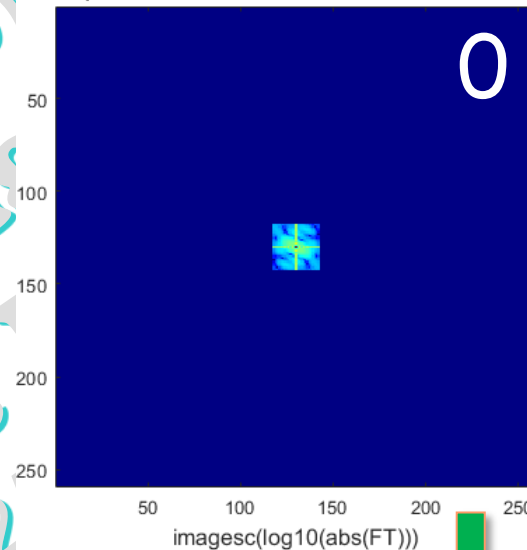
Reconstruction from reduced FT of size 129 x 129



reduction to  $(50\%)^2$

reduced Spectrum

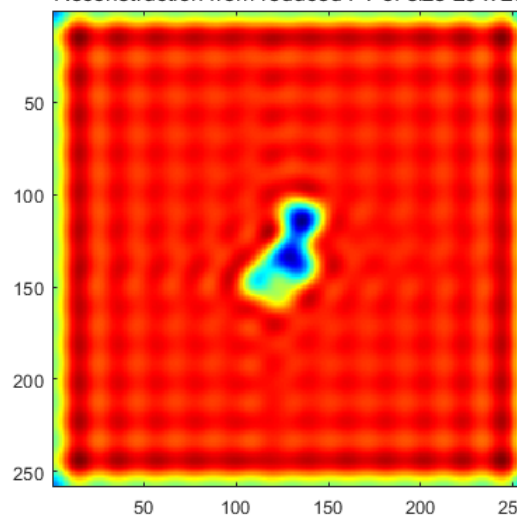
Spectrum of reduced FT of size 25 x 25



smaller window

reconstructed image

Reconstruction from reduced FT of size 25 x 25



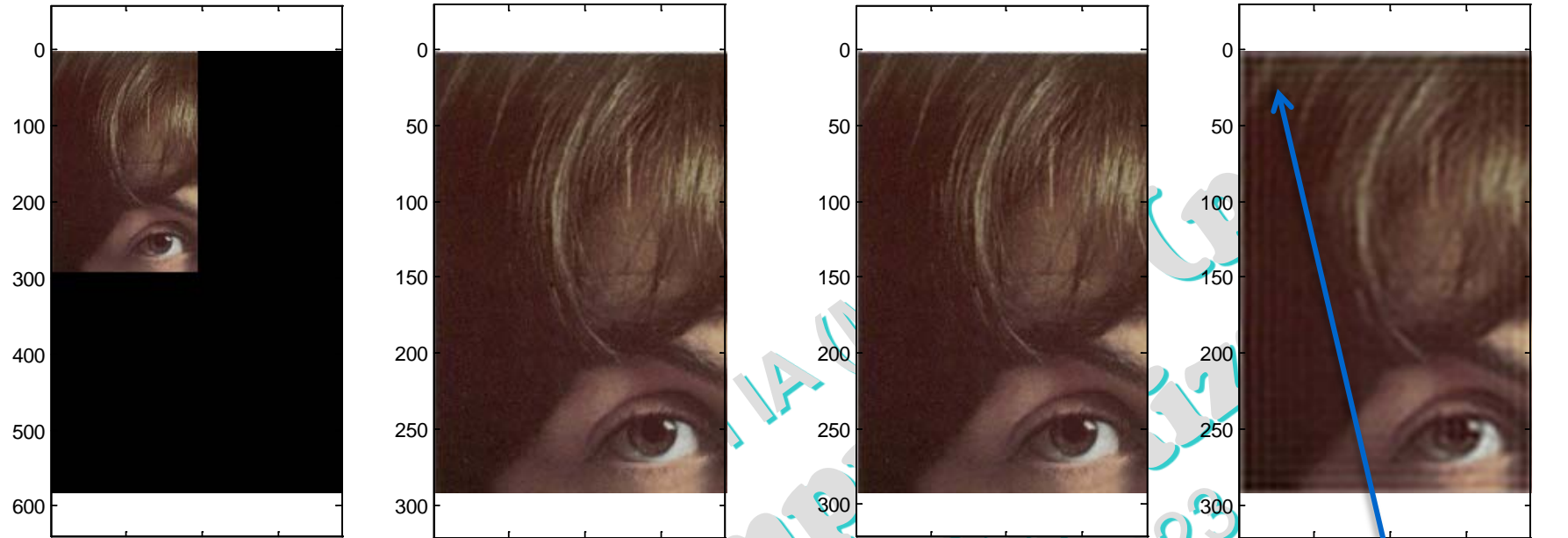
reduction to  $(10\%)^2$

# Example: windowing in frequency domain



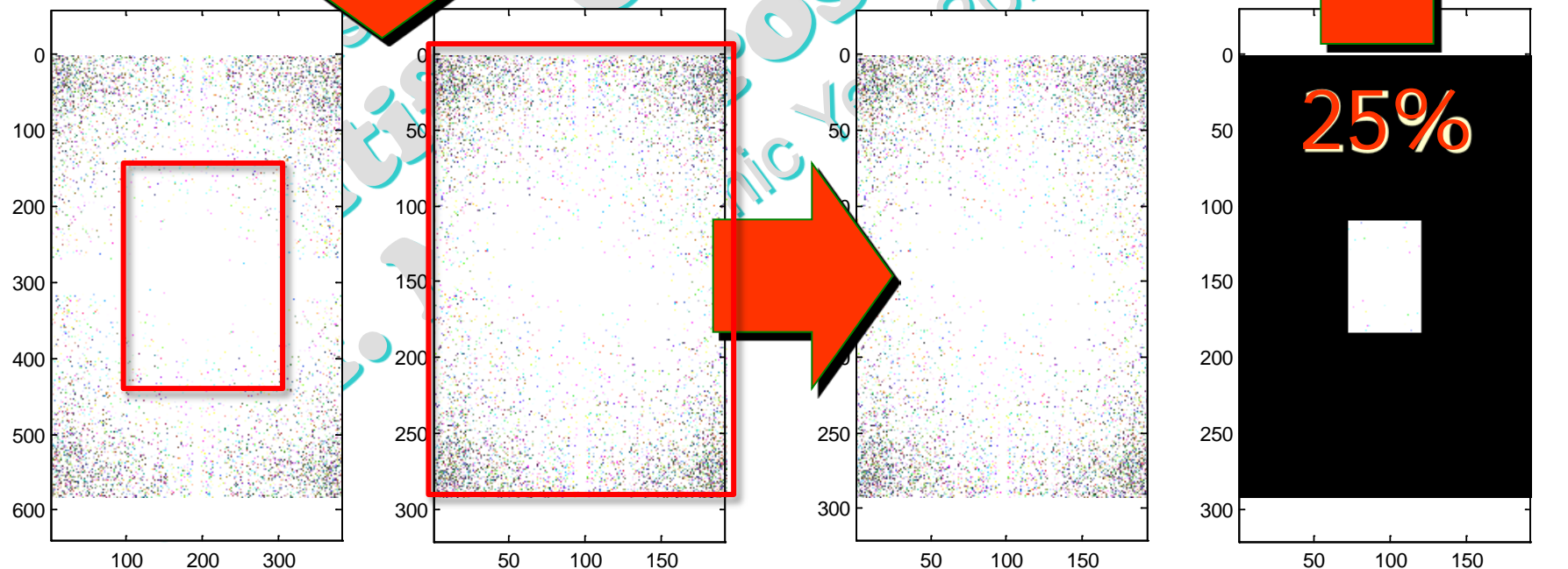
If the image is very large, you can divide it\* up into "small chunks", then process on every chunk (even in parallel), and at last reconstruct it from chunks by putting together results as a mosaic.

\* low-pass filtering



secondary oscillations

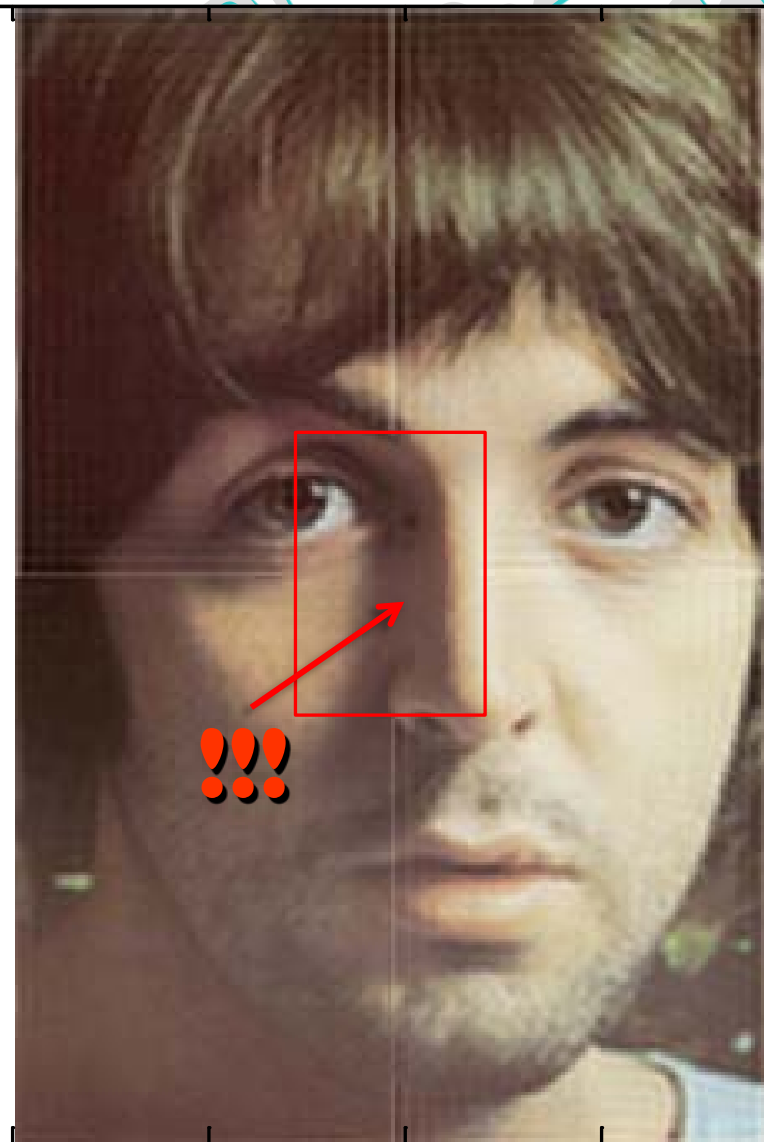
Fourier spectrum



25%

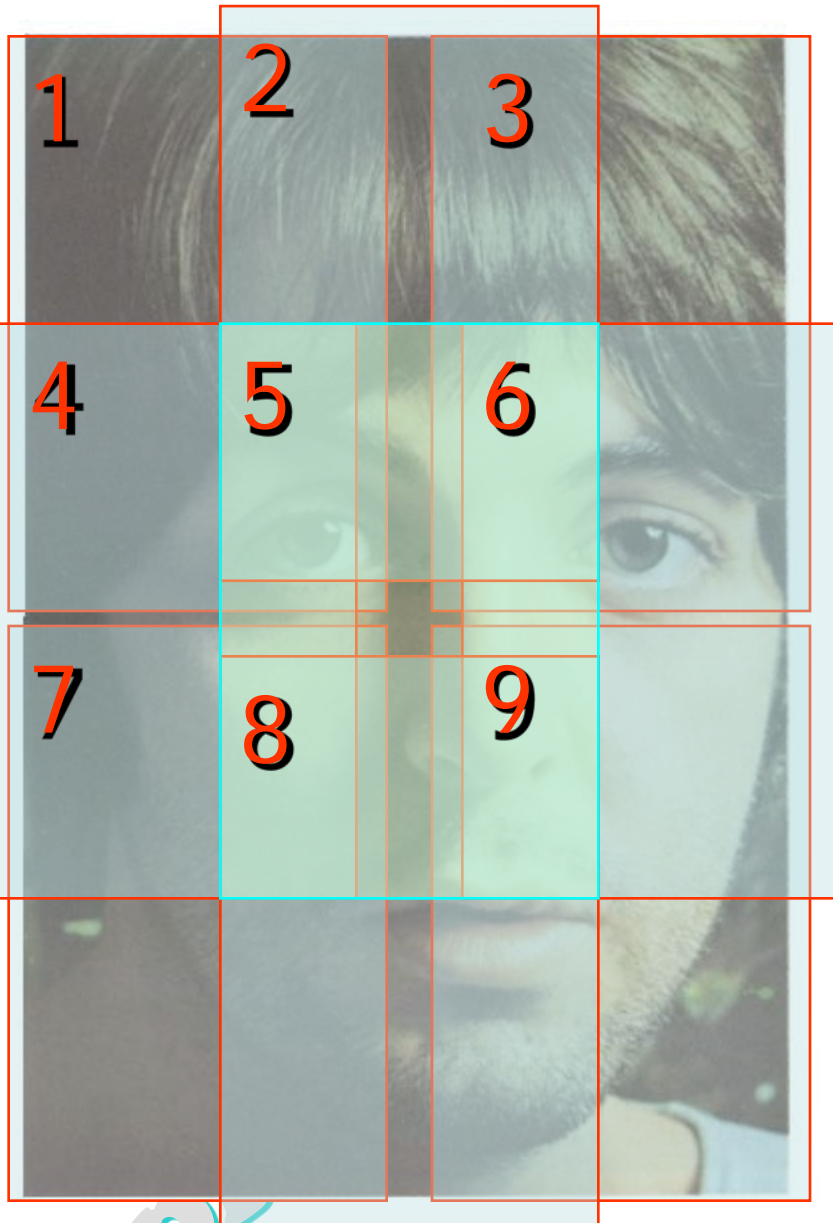
# Effects of windowing error

# How can it be removed?





# Windowing error: how can it be removed ?



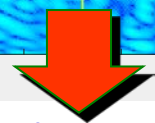
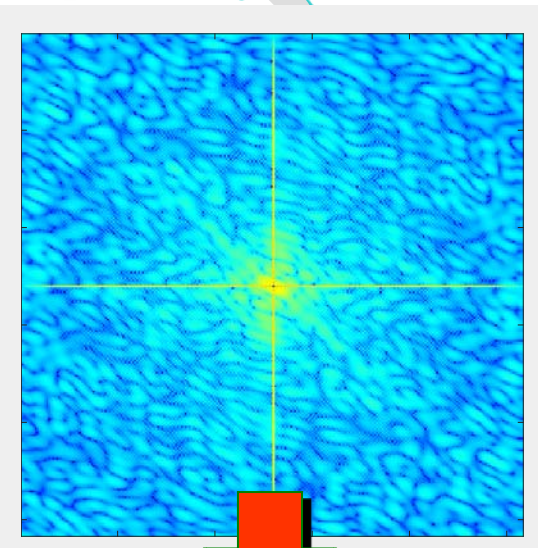
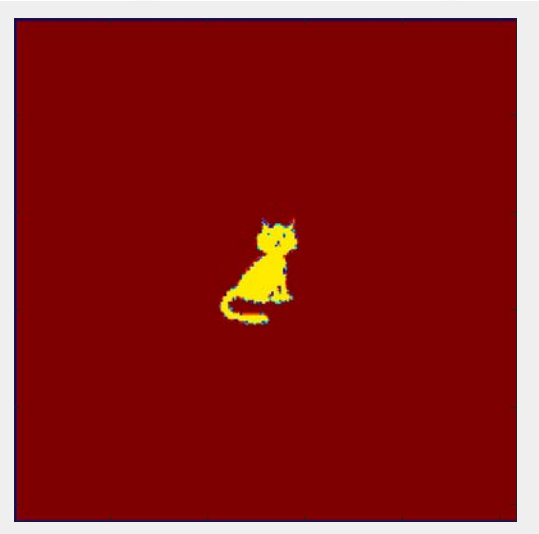
The image is divided into 3x3 subimages that overlap (in the example by 50%)

The reconstructed parts of the image after filtering can be cropped keeping only the central portion, free of errors and eliminating the border where the "windowing effect" occurs.

**Exercise:** Implement this algorithm in MATLAB.

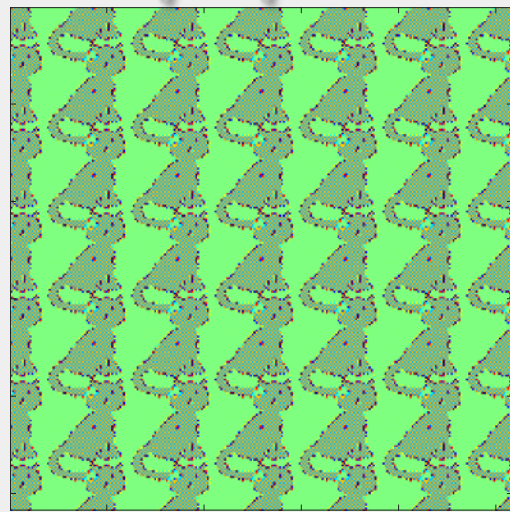
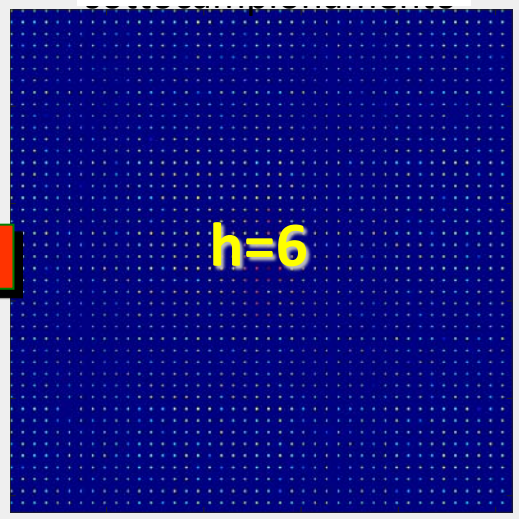
# Example: aliasing in frequency domain

```
f=imread('piccat.gif');  
[m,n]=size(f);  
F=fftshift(fft2(double(f)));  
FF=zeros(size(F));  
h=6; k=1:h:m; FT  
FF(k,k) = F(k,k); subsampling  
imagesc(log10(abs(FF)))  
axis ij; axis tight; axis equal  
colormap('jet')  
ff=fftshift(iff2(FF));  
imagesc(real(ff)); view(2)  
axis ij; axis tight; axis equal  
colormap('jet')
```



FT subsampling

superposition



Aliasing effect

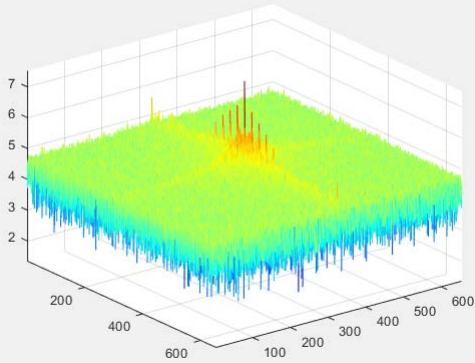
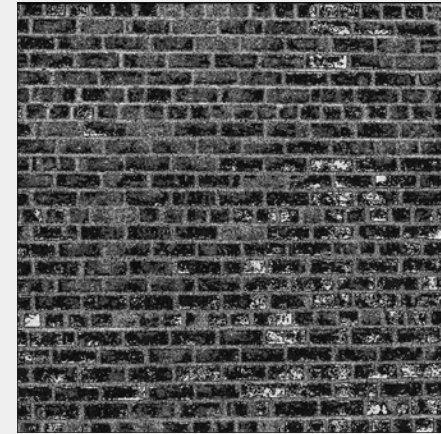
What is expected for  $h=3$ ? ... and for  $h=12$ ?

Only the values of FT with  $step=h$  in the two dimensions remain; the others are set to zeros.

# Example: periodic textures

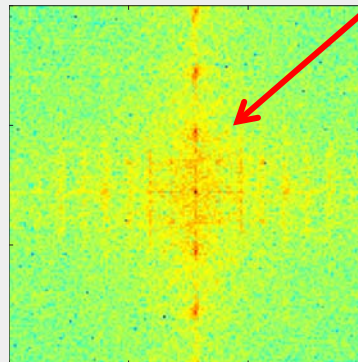
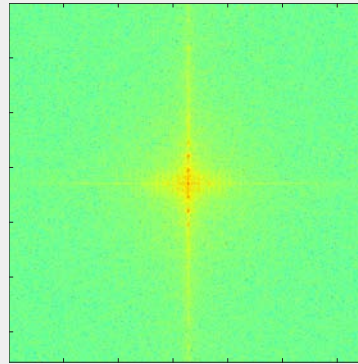
```
f=imread('./images/brick_wall.png');  
figure(1); clf; imagesc(f)  
axis tight; axis equal; colormap('jet')  
F=fftshift(fft2(f));  
figure(2); clf; mesh(log10(abs(F))); axis ij;  
axis tight; colormap('jet')  
figure(3); clf; imagesc(log10(abs(F)));  
axis tight; axis equal; colormap('jet')  
figure(2); AX=axis; % ZOOM  
AX(1:4)=[250 400 250 400]; axis(AX)  
figure(3); axis(AX(1:4))
```

brick\_wall.png

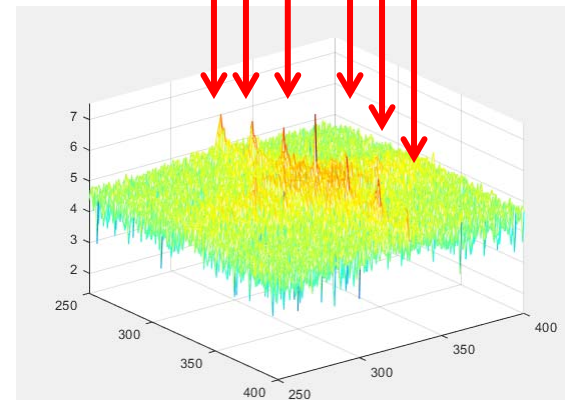


**zoom**

horizontal and vertical  
equispace peaks

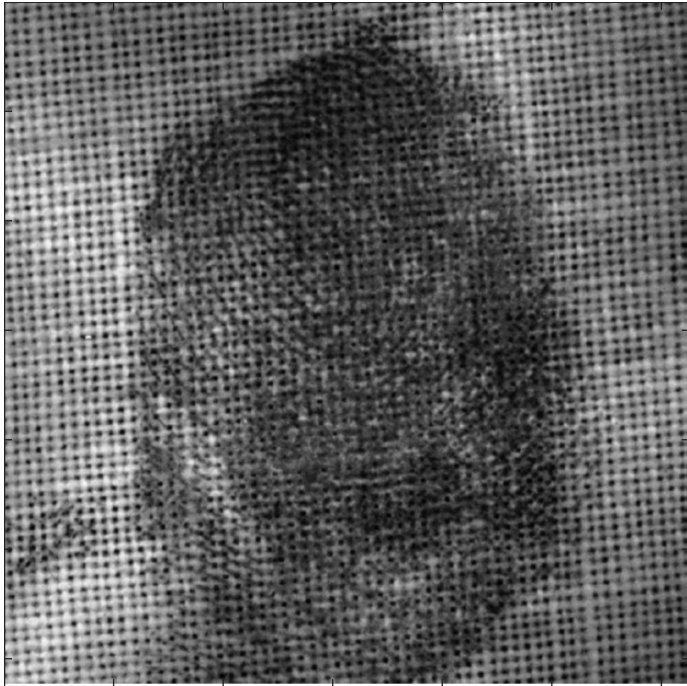


**peaks**

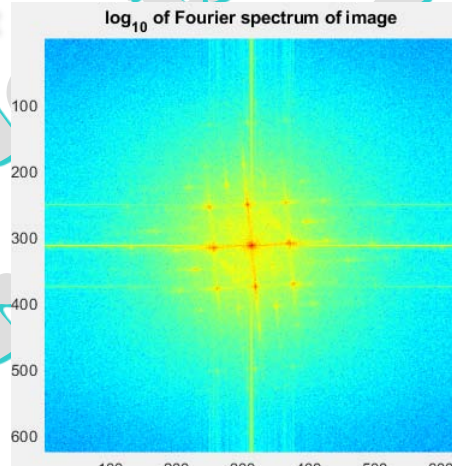


# Example: application of FT to images

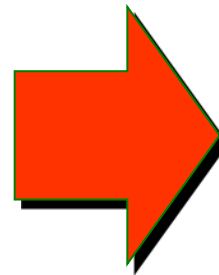
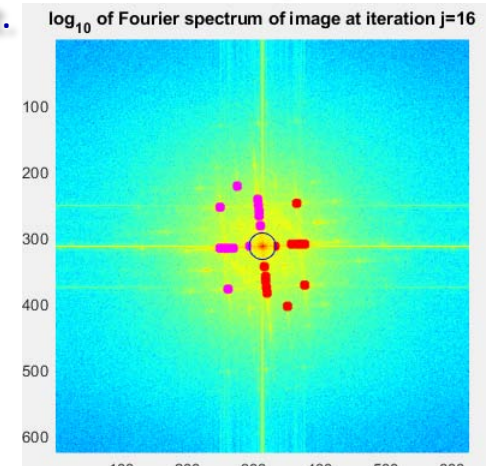
## Remove a periodic background

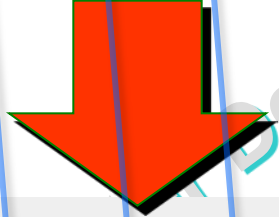
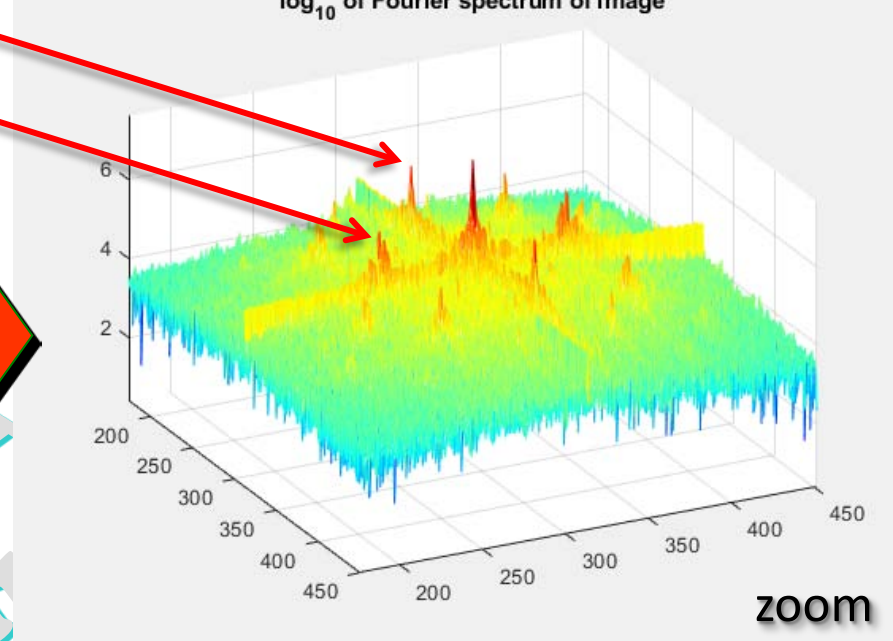
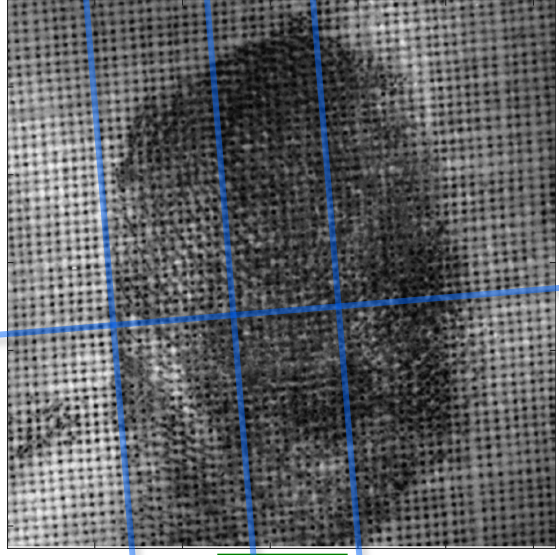


The background fabric texture interferes with the fingerprint

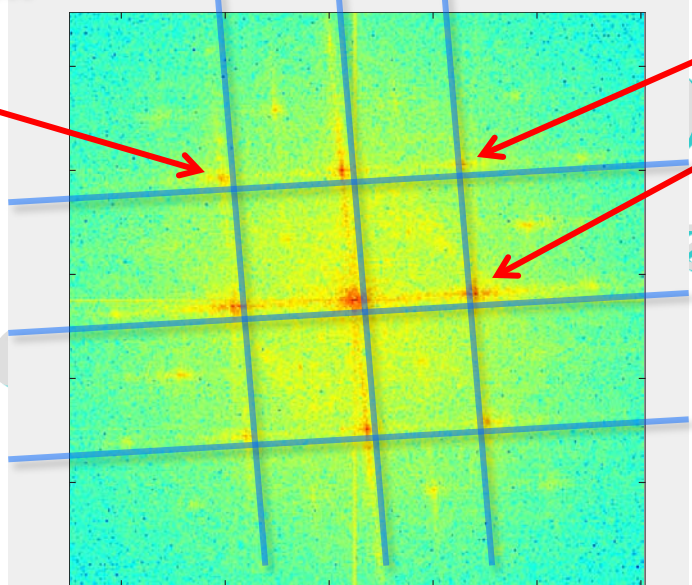


The fabric texture is now less visible, and the fingerprint stands out.



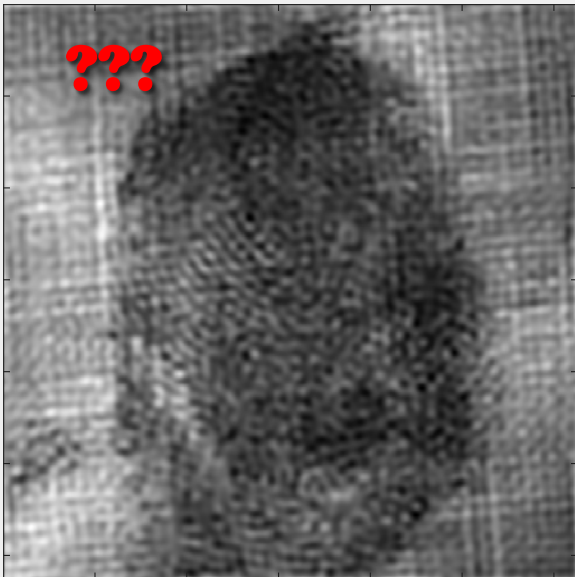
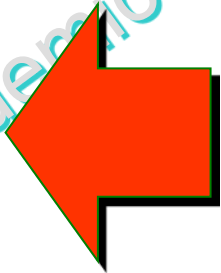
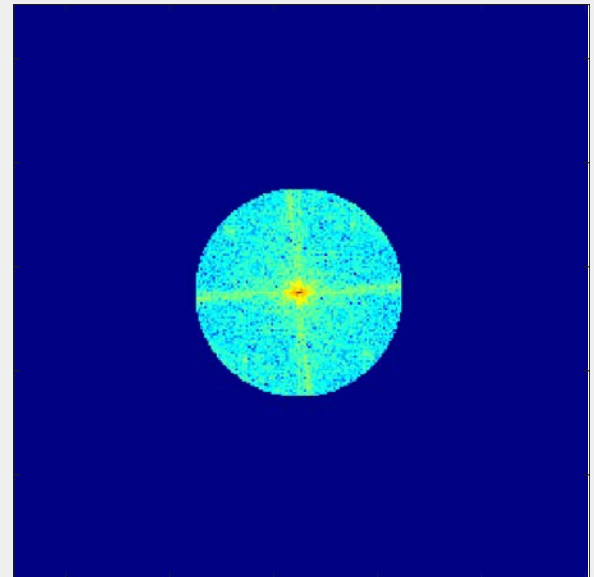
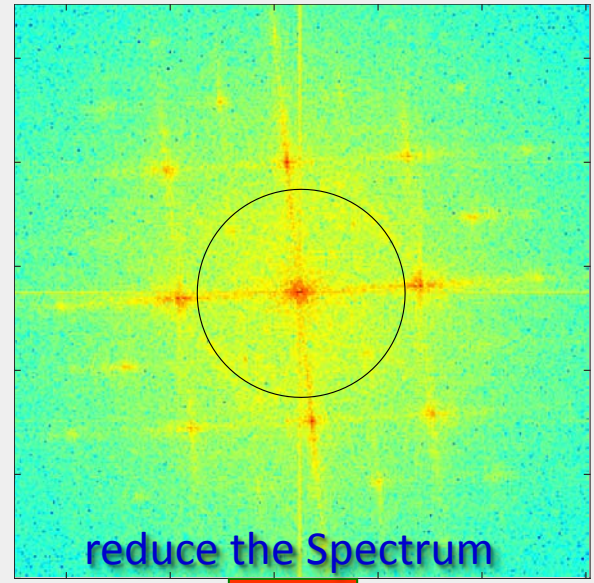
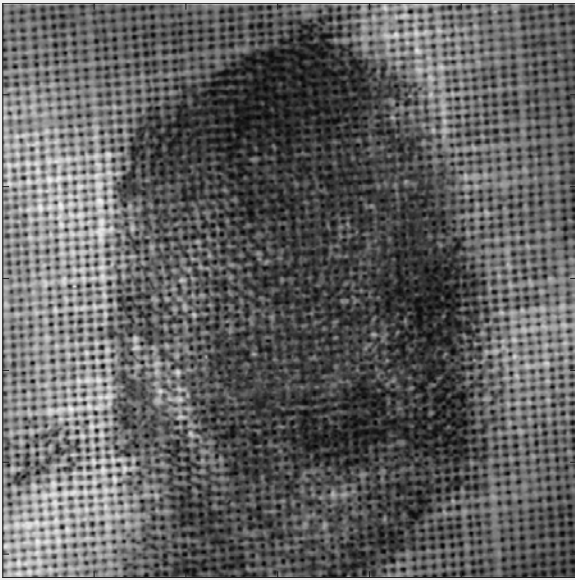


zoom



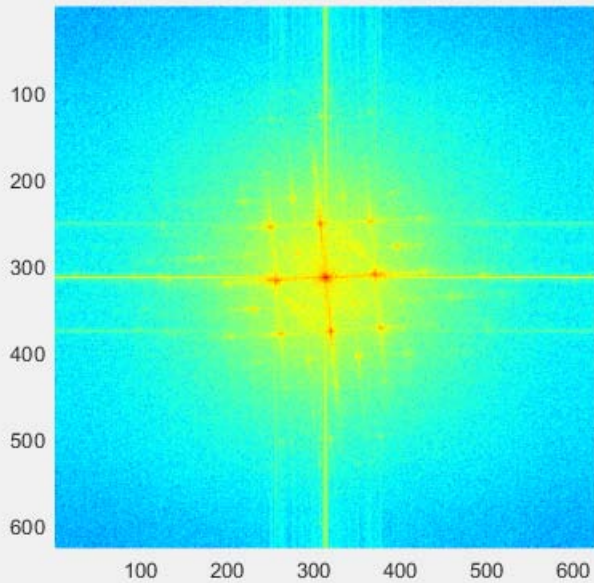
The **pulses** come from an oblique\* periodic signal: in the input image the **fabric texture** under the fingerprint is periodic. We need to remove these pulses.

\* see the rotation of the Spectrum equal to the rotation of the fabric texture.

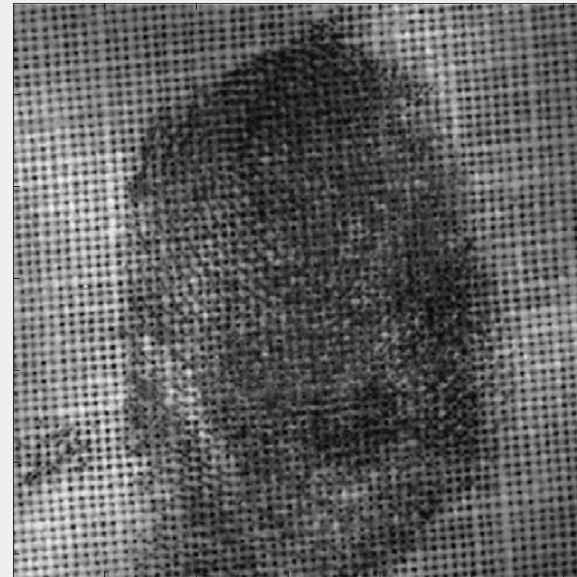
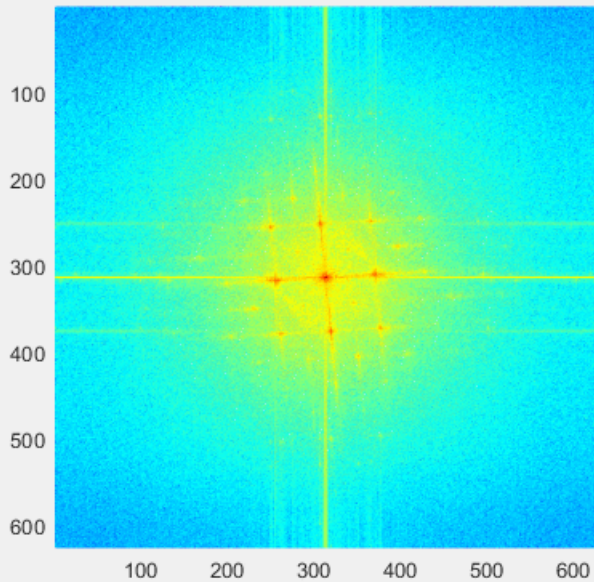


The **reduced Fourier spectrum** produces an image where both the fingerprint and the texture have lost their details

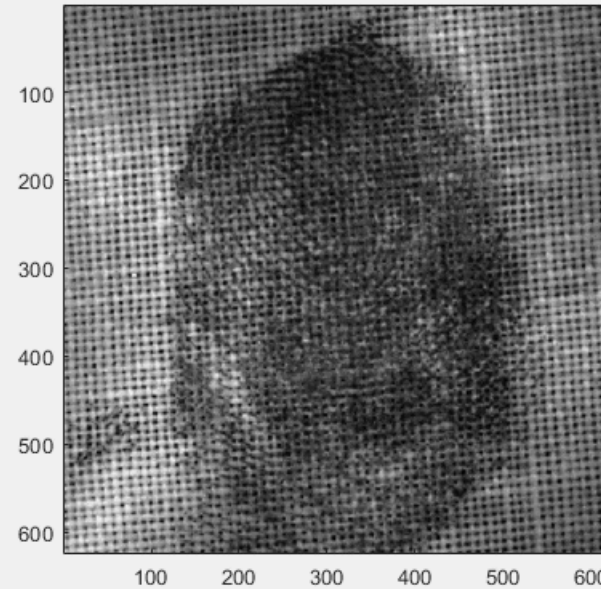
$\log_{10}$  of Fourier spectrum of image



$\log_{10}$  of Fourier spectrum of image

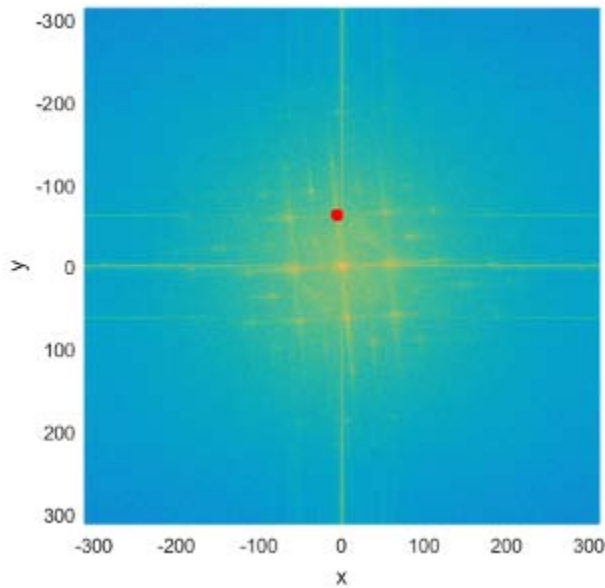


Original image



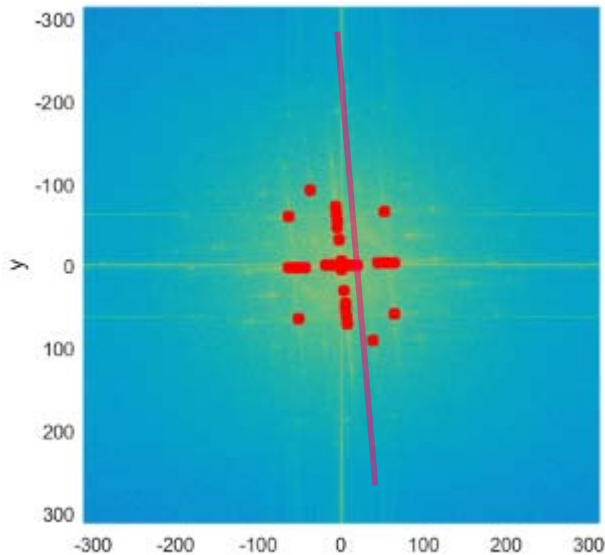
search peak points and set to zero the FT in the small disks

log<sub>10</sub> of Fourier Spectrum

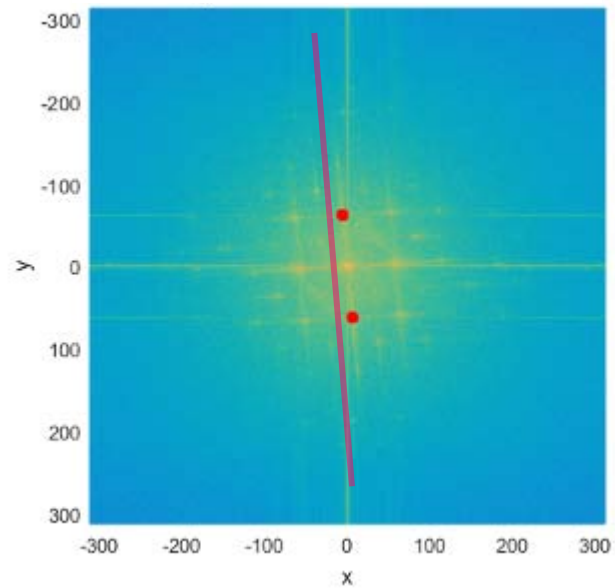


1) Remove frequencies within small circles around the pulse peak.

log<sub>10</sub> of Fourier Spectrum

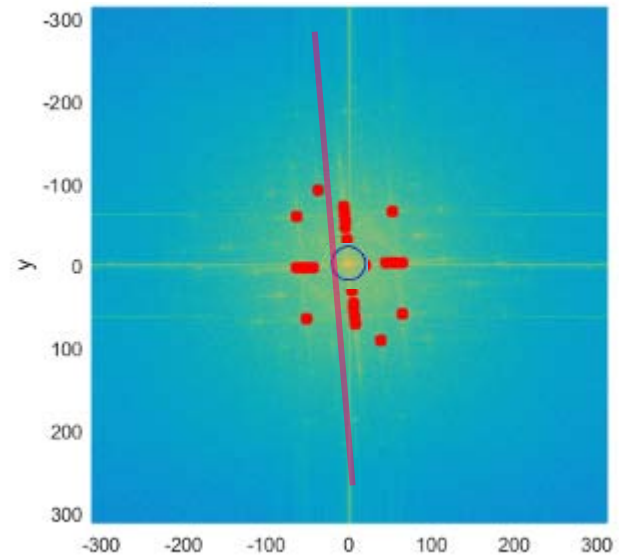


log<sub>10</sub> of Fourier Spectrum



2) Restore the central area of the spectrum.

log<sub>10</sub> of Fourier Spectrum



**Exercise:** Implement this algorithm in MATLAB.