

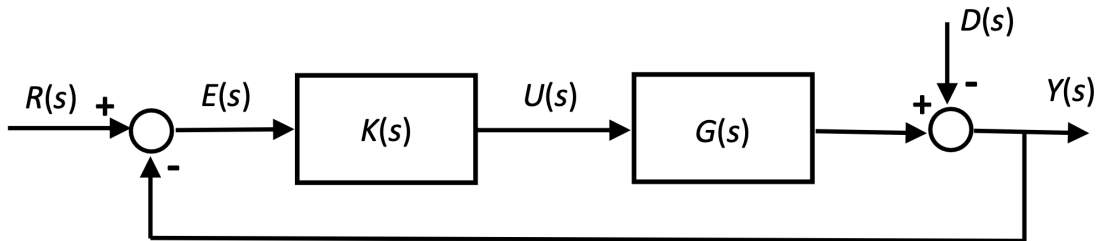
## Automatic Control Systems – May 9, 2024

Student: \_\_\_\_\_ ID: \_\_\_\_\_

1. Given the LTI system defined by the transfer function  $G(s)$ ,

$$G(s) = \frac{2(s + 20)}{(s^2 + 2s + 10)},$$

- calculate the analytic expression of the forced response to a step input of unitary amplitude (i.e., step response);
  - draw the qualitative step response.
2. For the closed loop system shown in figure,



where

$$G(s) = \frac{10}{(s^2 + 11s + 10)},$$

- devise  $K(s)$  in order to satisfy the following requirements:
  - $e_{\infty} = 0$  in the presence of both reference,  $r(t)$ , and disturbance,  $d(t)$ , step input signals;
  - $y(t)$  with overshoot  $s \leq 15\%$  to a step reference input  $r(t)$ ;
  - settling time  $t_{s5\%} \leq 1$  s;
- draw the qualitative response  $y(t)$  of the devised closed loop system to the following inputs:

$$r(t) = 1(t);$$

$$d(t) = 0.3 \cdot 1(t - 6).$$

**Time available: 2 hours**