



Course of
"Automatic Control Systems"
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Problems

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Problem 1.a

✦ *Compute the analytic expression of the step response of the following LTI systems:*

$$\bullet \quad G_1(s) = \frac{s+10}{s^2+6s+5}; \quad G_2(s) = \frac{s+20}{s^2+s+1}; \quad G_3(s) = \frac{-3(s-2)}{(s^2+4s+3)};$$

$$\bullet \quad G_4(s) = \frac{s+14}{s^2+10s+30}; \quad G_5(s) = \frac{s+24}{s^2+3s+45}; \quad G_6(s) = \frac{s+15}{s^2+9s+20}$$

✦ *Plot the step response for the different LTI systems*



Problem 1.b

✦ *Compute the transfer function of the following LTI system:*

$$\begin{aligned}\dot{x} &= \begin{pmatrix} 0 & 1 \\ a & -1 \end{pmatrix} x + \begin{pmatrix} 0 \\ 1 \end{pmatrix} u, \\ y &= (1 \quad 0)x\end{aligned}$$

✦ *Discuss the stability by varying $a \in (-\infty, +\infty)$.*

✦ *Plot the step response for the LTI system with $a = -4$.*



Problem 2

✦ *Study the frequency response of the following LTI systems by drawing the asymptotic Bode diagrams:*

$$\bullet \quad G_1(s) = \frac{s}{s^2 + 6s + 5}$$

$$\bullet \quad G_2(s) = \frac{s}{s^2 + s + 1}$$

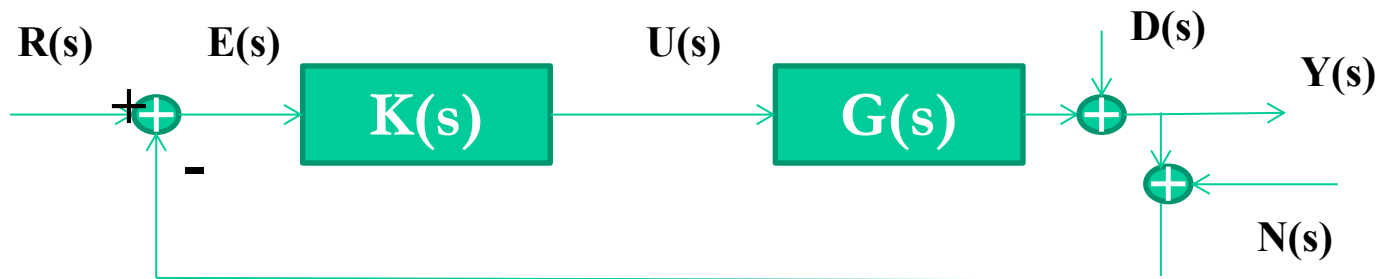
$$\bullet \quad G_3(s) = \frac{20(s + 0.1)}{(s^2 + 21s + 20)}$$

$$\bullet \quad G_4(s) = \frac{10(s + 3)}{(s + 1/3)(s + 9)}$$

$$\bullet \quad G_5(s) = \frac{10(s + 3)}{s(s + 1/3)(s + 9)}$$



Problem 3 - Controller design



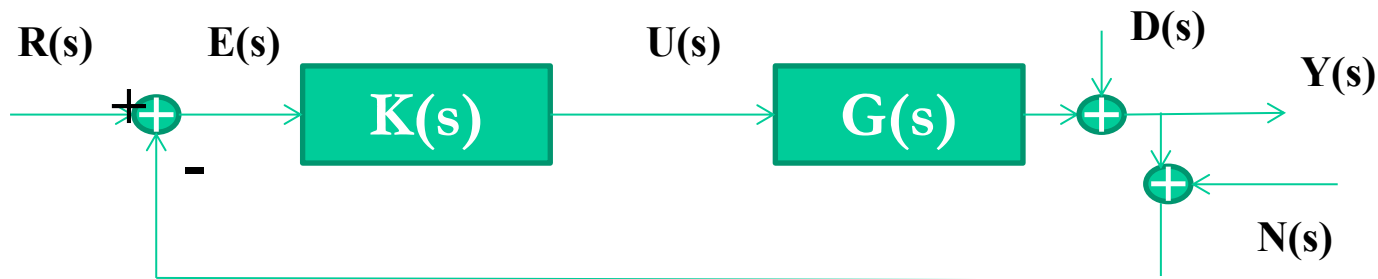
✦ *Stability*

✦ *Robust stability*

✦ *Steady-state performances*

✦ *Transient performances*

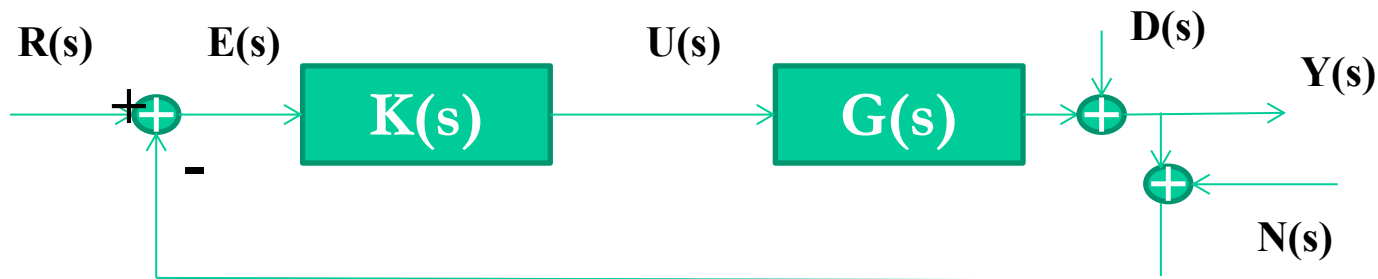
Problem 3 – Example 1



$$G(s) = \frac{1}{s^2 + s + 1}$$

- $e_{\infty r} \leq 10\%$ for a reference signal $r(t) = r_0 1(t)$
- Overshoot $s \leq 30\%$
- Settling time $t_{s5\%} \leq 1s$

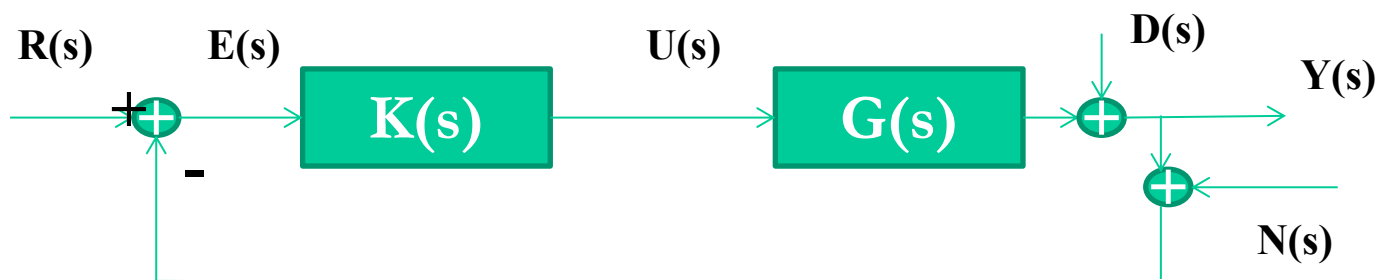
Problem 3 – Example 2



$$G(s) = \frac{1}{s^2 + s + 1}$$

- $e_{\infty} = 0$ for a reference signal $r(t) = r_0 1(t)$
- Overshoot $s \leq 30\%$
- Settling time $t_{s5\%} \leq 2s$

Problem 3 – Example 3



$$G(s) = \frac{4}{(s+4)(s+2)}$$

1. Devise a controller $K(s)$ with the aim to satisfy the following requirements:
 - $e_{\infty,r} < 10\%$ for a reference signal $r(t) = r_0 1(t)$;
 - overshoot $s \leq 30\%$.
2. Compute the gain and phase margins of the open loop function for $K(s)$ devised at 1).
3. Plot the resulting step response of the closed loop system.