



Ducting

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Tropospheric ducting

Electromagnetics and Remote Sensing Lab (ERSLab)

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Strait of Messina

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FATA MORGANA IN THE STRAIT OF MESSINA (1773), MESSINA REGIONAL LIBRARY



How it works

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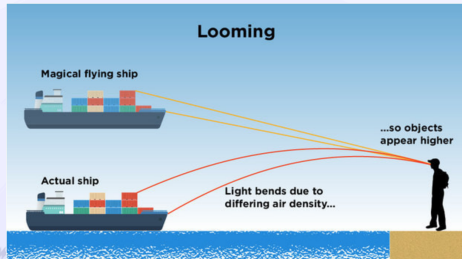
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Fata Morgana mirage

- Light bends downward when entering colder (denser) air due to the larger refractive index.
- We naturally assume light rays taking a straight path from the true object to our eyes.



UFO?...

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Photographs from the hamlet of Gillan, near Falmouth



No...Fata Morgana



A key issue in maritime radar

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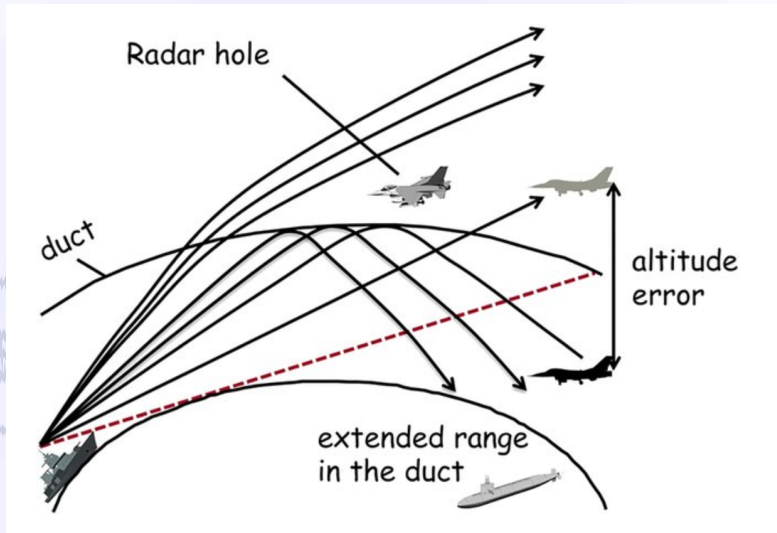
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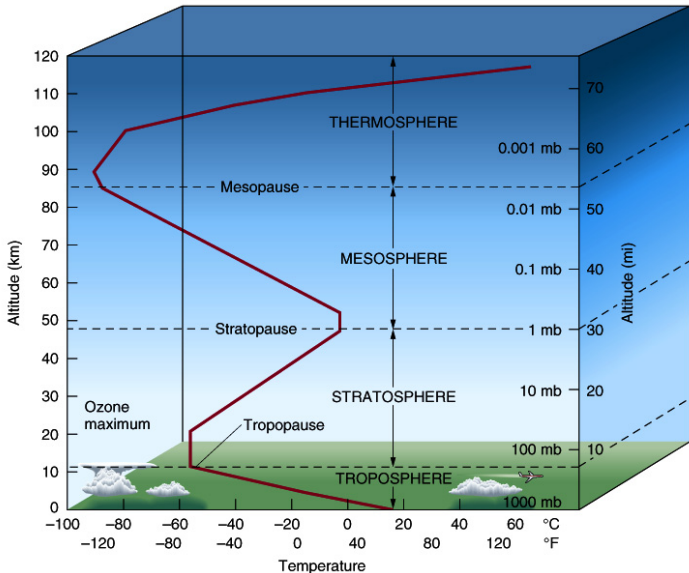
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$$\epsilon = \left(\epsilon - j \frac{\sigma}{\omega} \right) = \epsilon' - j\epsilon''$$

ϵ'

- Refraction
- Diffraction
- Depolarization
- Reflection
- DUCTING

ϵ''

Absorption by:

- Atmospheric gases
- Hydrometeors

The real part of the index of refraction, n , is here accounted for.



Stratified atmosphere

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Variations of the index of refraction

- We focus on the lowest part of the atm, namely the troposphere, which extends up to 14km asl.
- Variations of the refraction index involve both variations of the mean refractive index (causing bending) and fluctuations due to turbulence (scintillation, lensing).
- Here we focus on **variations in the mean refraction index** that are largest in the vertical direction.
- The troposphere is assumed to be **horizontally stratified**.



Index of refraction

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Debye's formula

- The index of refraction can be expressed as a function of the atmospheric pressure P , water vapor pressure e and temperature T :

$$n = 1 + 77.6 \times 10^6 \frac{P}{T} + 0.373 \frac{e}{T^2} \quad (1)$$

Characteristics of n

- The index of refraction rarely exceeds 1.0004 at the surface.
- Radiowave propagation, as pointed out by GO theory, depends mainly on the gradient of the refractivity index.



Radio refractivity index N

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- The behavior of n in the atm is such that it is more convenient to define the **radio refractivity index** N :

$$N = (n - 1) \times 10^6 \quad (2)$$

- The International telecommunication Union (ITU), defined a standard atm in terms of N , proposing an exponential decay of N with the height above the ground z

$$N = N_s e^{-\frac{z}{H}} \quad (3)$$

- An alternative index - **termed as modified refractivity** M - is also very common in radio propagation. It includes the Earth's curvature.



Standard atmosphere

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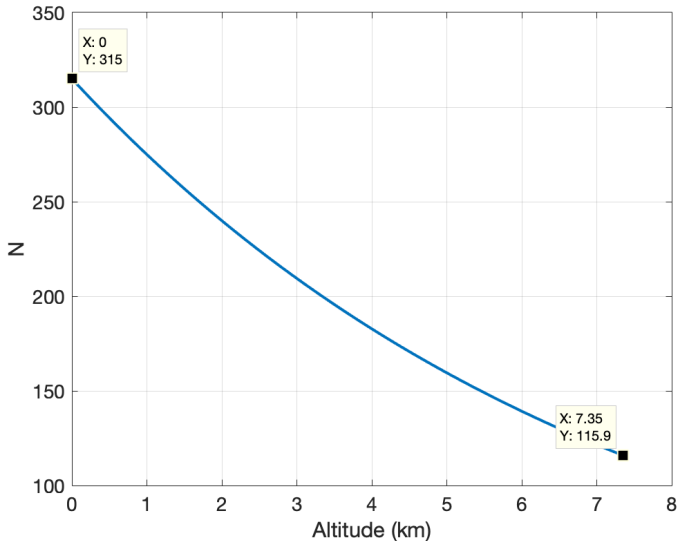
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Geometric optic

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The Geometric optic approximation

GO suggests that a wave propagating in a medium calling for a gentle n variability bends according to the portion of the gradient of n transverse to the direction of the ray travel.

- According to GO, the ray curvature ρ is given by:

$$\frac{1}{\rho} = -\frac{1}{n} \frac{dn}{dz} \cos \alpha \quad (4)$$

- which, assuming $n \approx 1$ and for small α angle, can be equivalently rewritten in terms of refractivity:

$$\frac{1}{\rho} = -\frac{dn}{dh} = -\frac{dN}{dz} 10^{-6} \quad (5)$$



Bending in the standard atm

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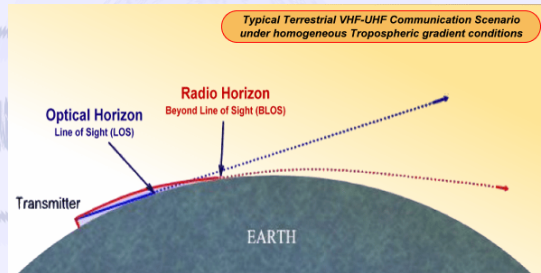
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- In the first kilometer of the standard atm eq.(3) can be linearized and N calls for a constant decreasing trend of -43 [N/km]
- This results in **a ray that bends towards the Earth extending the optical horizon:**





Anomalous propagation

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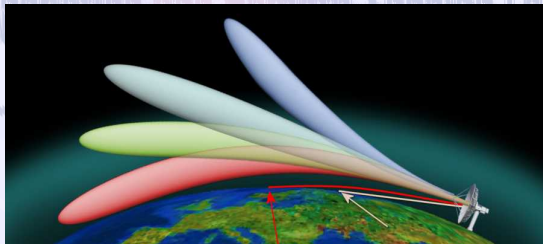
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Anomalous propagation

Non-standard or anomalous propagation occurs when the refractive index is modified in a way that is different by the standard atmosphere.

- This may be due to changes in temperature gradient, pressure or water vapor content.
- A wide range of non-standard propagation conditions may apply.





Anomalous propagation

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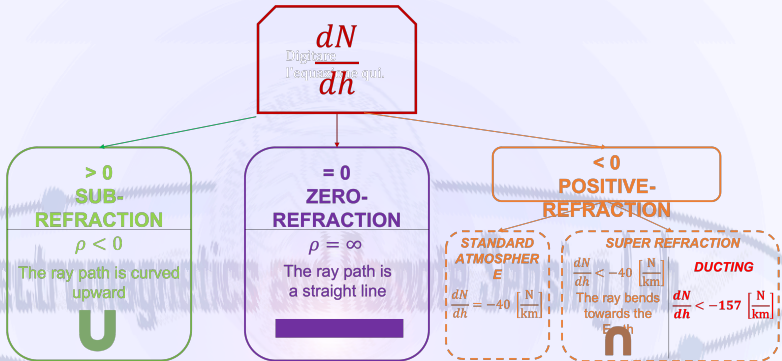
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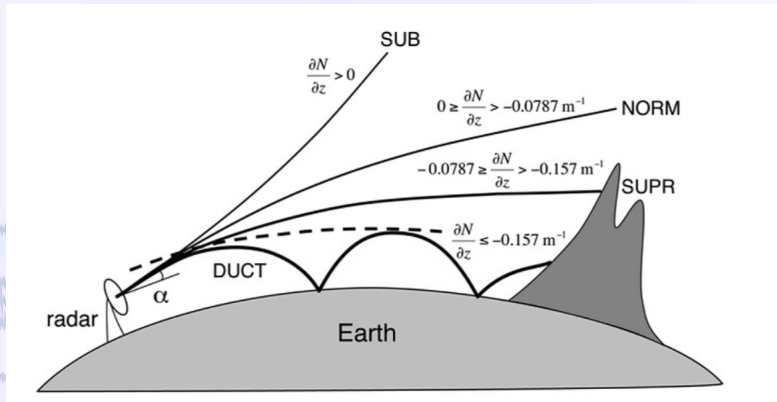
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- It is an anomalous propagation mechanism that occurs in case of sharp N variations.
- This may happen in two cases (or a combination of both):
 - a sharp decrease in vapor pressure with height;
 - a temperature inversion, i.e.; the temperature increases with height.
- **Temperature inversion is the dominant factor.**



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Temperature inversion

- Under normal atmospheric conditions, the warmest air is found near the surface of the Earth.
- The air gradually becomes cooler as altitude increases.
- An unusual situation can develop in which layers of warm air are formed above layers of cool air.

This condition is known as temperature inversion

These temperature inversions cause **channels, or ducts**, of cool air to be sandwiched between the surface of the Earth and a layer of warm air, or between two layers of warm air.



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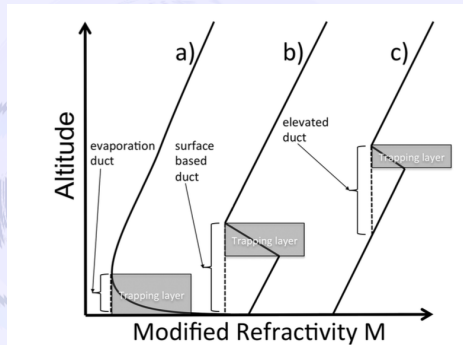
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According to the mechanisms that determine the duct's formation, different types of ducts can be observed





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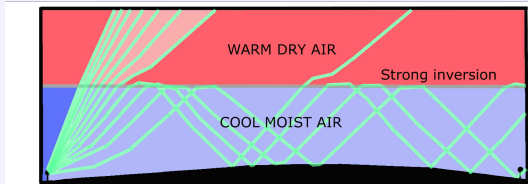
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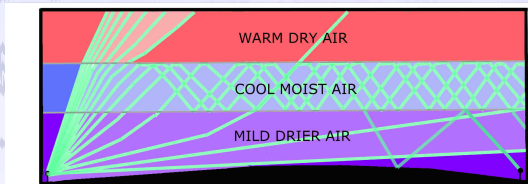
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surface duct



elevated duct



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Beyond-LoS propagation

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Under ducting conditions:

- The signals do not spread isotropically through the atmosphere but they mostly spread in the ducting layer.
- This implies a spreading loss that decreases considerably compared to the standard atmosphere.

In this way, the trapped signals can travel over the horizon, making the ducting layer convenient for beyond-line-of-sight (b-LoS) communications.



b-LoS

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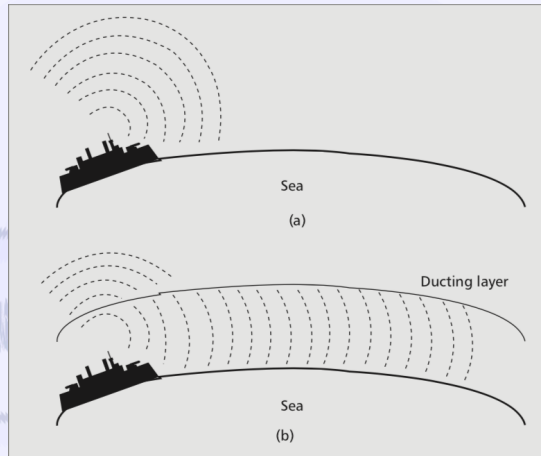
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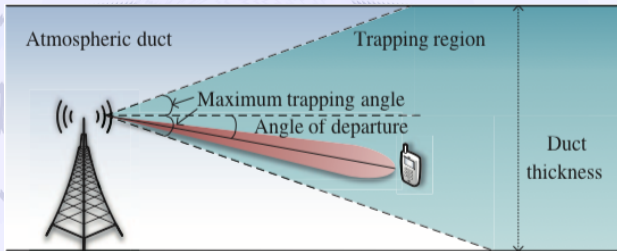
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For a wave to be trapped:

- The maximum trapping angle should be small (≈ 0.4 degree).
- The minimum trapping frequency is around 300MHz.





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Alex Mahalov and Austin McDaniel *Long-range propagation through inhomogeneous turbulent atmosphere: analysis beyond phase screens*
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