$$f_b = T\frac{df_0}{dt} = \frac{2R}{c}\frac{df_0}{dt}$$